

Quelques approches formelles pour tester la robustesse de processus de reconstruction de réseaux

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Network inference

Goal Identify the **main actors and functions** involved in the response of a system.

Methods

- **Data-mining**. Statistics. Machine Learning...
- **Metaheuristics**. Search for a local optimal (genetic algorithms...).
- **Optimization**. Look for best-score solution (ILP).

Most approaches are **discriminative:
their output is a "single" most-probable solution.**

Uncertainties appear at different stages of the identification process

- **Confidence** in the resulting predictions?
- Relevance of a **unique** solution?

Explore complete space of solutions?

Large range of inferred properties

- **Topological structure.** Transcriptional or metabolic network.
- **Discrete dynamics.** Logical rules
- **Continuous dynamics.** Parameter estimation.

Fluctuations in data

- Qualitative observations.
- Scoring of errors.

Is it possible to study the set of (sub)-optimal solutions?

→ **Enumeration, sampling ?**

→ **Formal methods?**

Enumeration...

Explore the space of solutions to combinatorial optimization problems which are relevant in system biology

Integer Linear Programming?

- **Systems biology**. Used in many frameworks (metabolism).
- **Diffusion**. Few software tools.
- **Expert level required**. Small modifications induce loss of efficiency.

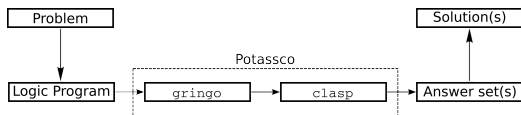
Declarative logics? (Prolog, Inductive Logic Programming...)

- **Systems biology**. Used mainly for experiment design.
- **Diffusion**. Appropriate flexibility.
- **Bad for enumeration**. Not scalable !!

→ **Find a compromise between efficiency and flexibility in the problem statement?**

Answer Set Programming: *what?* instead of *how?*

- Declarative logical problem solving paradigm
- Knowledge representation and reasoning problems
- **Combinatorial search problems in NP**



Potassco: **Potsdam** Answer Set Solving Collection

<http://potassco.sourceforge.net>

Rich modeling language

- Encoding problems as **queries on propositional logical programs**.
- *Gringo* grounder

Highly efficient inference engines

- **Boolean constraint** solving technology
- *Clasp* solver
- Competing with the power of SAT algorithms.

Short description

Disjunctive rules

$$\underbrace{k \{ a_1; \dots; a_n \}}_{\text{head}} \mid \underbrace{:- a_{n+1}, \dots, a_r, \text{not } a_{r+1}, \dots, \text{not } a_s}_{\text{body}}$$

- **Atoms.** $a_1 \dots a_n$ can be considered as facts.
- **Deduction**

Whenever all facts of the body are satisfied, one fact of the left part shall be true.

- **Integrity constraint.** " $\leftarrow a$ " is always false
- **Constraint.** " a ." is always true.

Answer Set

- Set of atoms satisfying all logical rules
- Minimality and stability properties
- Every atom of an answer set appears in the head of at least one rule.

Qui a tué le docteur Lenoir ?

Program

```
3 { nom, arme, pièce } 3
1 { Colonel Moutarde, Mademoiselle Rose } 1 :- nom
1 { chandelier, revolver } 1 :- arme
1 { cuisine, hall, salon, salle à manger } 1 :- pièce
1 { cuisine, hall, salon } 1 :- Colonel Moutarde
Salon :- Colonel Moutarde, not revolver
:- cuisine
Chandelier
```

Answer Sets??

Qui a tué le docteur Lenoir ?

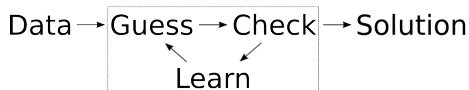
Program

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1 { cuisine, hall, salon } 1 :- Colonel Moutarde
Salon :- Colonel Moutarde, not revolver
:- cuisine
Chandelier
```

Answer Sets??

- Colonel Moutarde, salon, chandelier
- Mademoiselle Rose, salle à manger, chandelier
- Mademoiselle Rose, salon, chandelier
- Mademoiselle Rose, hall, chandelier

Guess & Check methodology



- **Data:** PKN and phospho-proteomics dataset (facts)
`node(tnfa). node(p38). edge(tnfa,p38,1). exp(1,tnfa,1). obs(1,p38,0).`
- **Guess:** Generate candidates models (non-deterministic)
`{clause(A,N)} :- hyperedge(A,N).`
- **Check:** Eliminate invalid models (integrity constraints)
`:- clause(A,N), clause(B,M), A!=B, redundant(A,B).`
- **Learn:** Loop between "guess" and "check"
- **Optimize:** Minimize cost function (weighted sum of atoms)
`#minimize[mismatch(E,R,W) = W, clause(A,N) : param(P) = N*P].`

Ongoing issue

ASP technologies are now proved to be mature and very efficient in several computational issues.

→ *constraint satisfaction, diagnosis, repairing, planning...*

Is ASP useful in systems biology?

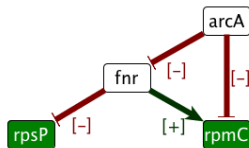
Work in progress...

- Consistency checking of network
- Inference of logical rules for signaling networks
- Inference of robust regulatory nodes
- inference of metabolic network

Validation/Correction of (possibly inferred) networks

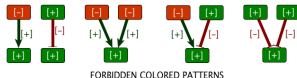
Knowledge-representation

- **Regulations.** Signed oriented graph.
- **Edge colors.** Regulatory effects.
- **Node colors.** Expression data.



Constraint over graph-coloring

- **Causal law.** Explain the expression of each target gene by the consistent regulation of a source
- **Forbidden patterns.**



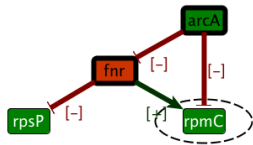
ASP encoding

```
vertex(rpsP). vertex(fnr).  
vertex(arcA). vertex(rpmC).  
edge(fnr,rpsP). observedE(fnr,rpsP,-).  
edge(fnr,rpmC). observedE(fnr,rpmC,+).  
edge(arcA,fnr). observedE(arcA,fnr,-).  
edge(arcA,rpmC). observedE(arcA,rpmC,-).  
observedV(rpsP,-). observedV(rpmC,-).
```

```
labelV(I,+); labelV(I,-) ← vertex(I).  
labelV(I,S) ← observedV(I,S).  
labelE(J,I,+); labelE(J,I,-) ← edge(J,I).  
labelE(J,I,S) ← observedE(J,I,S).  
receive(I,+)  
← labelE(J,I,S), labelV(J,S).  
receive(I,-)  
← labelE(J,I,S), labelV(J,T), S≠T.  
← labelV(I,S), not receive(I,S).
```

Results [Guziolowski-BMCGenomics'09, Gebser-KR'10]

- **Prediction.** *rpsP* and *fnr* have fixed colors according to allowed patterns.
- **Diagnosis.** An extra forbidden pattern appears on *rpmC*.
- **Correction.** Also possible.

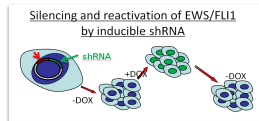
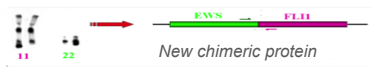


The expression of *rpmC* cannot be explained.

Example of application

Ewing Sarcoma

- Chimeric protein
- **Institut Curie**. Inactivation of the protein expression.



Data [Institut curie. Barillot & Delattre]

- Literature-based regulatory network
- Time-series genes expression after the protein inactivation



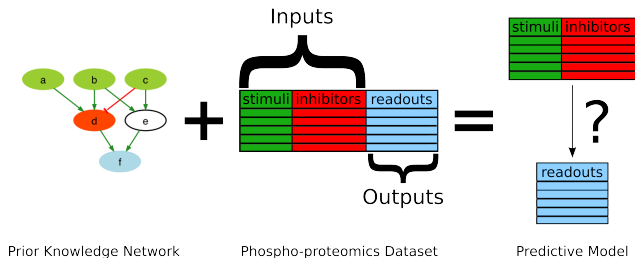
→ **What can be surely predicted from this information?**

Learning logical static rules

Data

- Signed and directed causal interactions among proteins
- Phosphorylation activity in time t after stimulation

Goal Predictive models of immediate-early protein signaling pathways

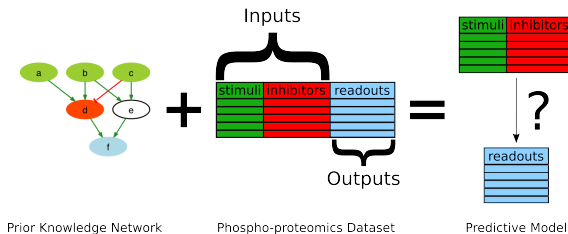


Underlying assumptions

- Focus on fast reactions
- No time for feedback mechanisms
- Pseudo-steady state assumption

Predictive Signaling Network Challenge [Prill'11].

12 groups with different formalisms (ODEs, machine learning, boolean logic)

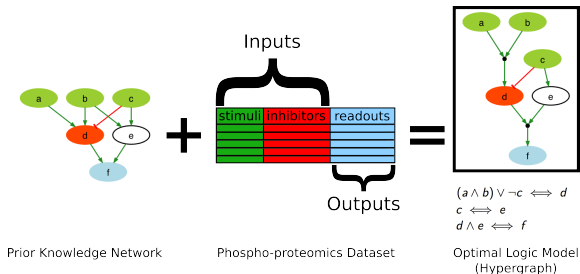


Score Trade-off between fitness and model size.

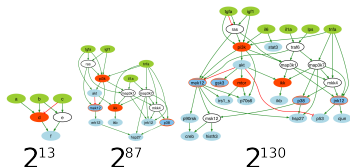
- **Biological Property:** consistency with experimental data
- **Parsimony Principle:** minimal/simplest explanation

Discrete approach

Optimization Learning **Logic** Models or **hypergraphs**?



Search space. Hypergraphs compatible with the graph ($2^{\#hyperedges}$)



State-of-the-Art CellNOpt [Saez-Rodriguez'09]

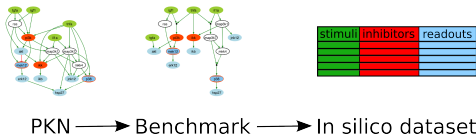
- **Genetic algorithm** to train logic models
- **Weaknesses** **Guarantee to find all global optimal models? Scaling?**

Comparing meta-heuristics and declarative logics



Benchmark and comparison sets

- **2 real cases.** Middle and large-scale with discretized real dataset.
- **240 in-silico cases.** middle-scale, several benchmarks and in-silico datasets.



Criteria of comparison

- Success / Completeness
- Time performance

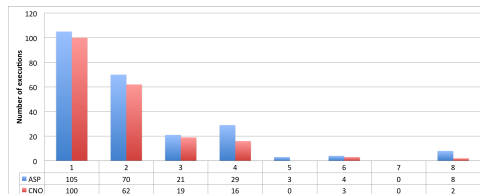
Success / Completeness

Discretized real datasets [Videla-CMSB'12]

Optimal models	ASP	CellNOpt
Middle	8	2
Large	2	0

- Several optimal models.
- Metaheuristic miss all optimals in the large-scale case.

Generalization: 240 in-silico studies [Videla-CMSB'12]



- No single optimal model in more than 60% of studies.
- Metaheuristics fail in identifying all optimal when they are numerous.

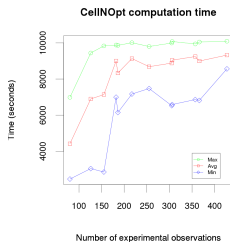
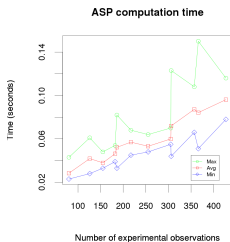
Time performance

Discretized real datasets

- **Metaheuristics are perturbed by the identification of global optimal models**

Times	ASP (s)	CellNOpt (h)
Middle	0.09 seconds	9.2 hours
Large	0.5 seconds	27.8 hours

Generalization: 240 in-silico studies



- **Significant improvement in computation times**

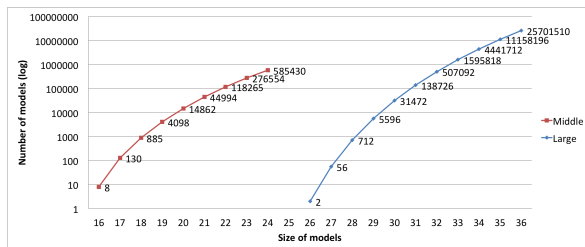
Analysis of incompleteness

Metaheuristics

	Number of saved models	Size	Minimal size
Middle	66	16→24	16
Large	206	27→36	26

- CNO finds suboptimal models “close” to optimal models
→ Are they a good representation of the space of sub-optimal models?

Space of sub-optimal models?



- **ASP allows enumerating** the space of suboptimal models
- **Exponential growth** with the size
- *No information on the representativity of CNO models*

Impact of real data? Space of sub-optimal models?

Real case *[Videla-Work in progress]*

- Numerical value → 100-value discretizations !
- Loops → new encoding
- **Good time performances**

(Non)-unicity of solutions

- **Still several optimal solutions**
- Combinatorics: **mutual exclusive patterns.**

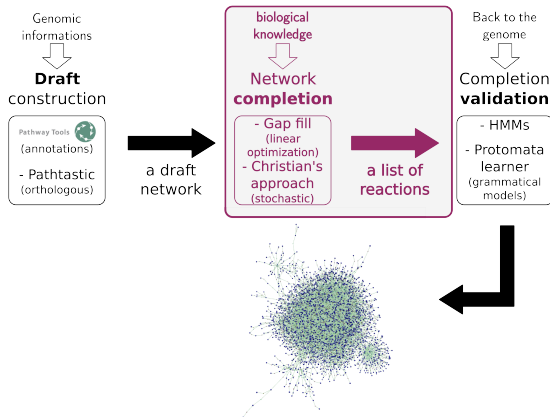
Including noise? *[Guziolowski-Work in progress]*

- A 10% noise over real data is **inherent** to the technologies.
- **Enumeration: more than 10000 sub-optimal models**

→ **Relevance? Strong need for biological metrics to select models!**

Quite troubling...

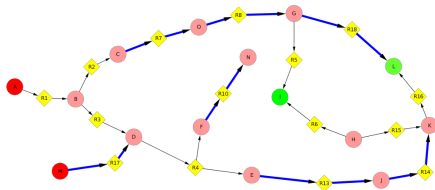
Optimization methods → Metabolic network completions



Hints on the number of possible completions?

Optimization-based methods

Cardinal minimal completion Add the minimal number of reactions to explain the presence of metabolites.



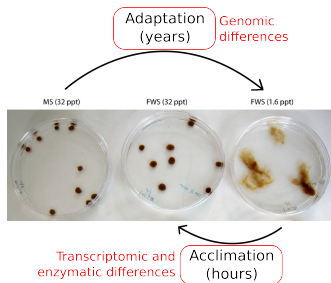
Linear programming: GapFill [Kumar'07]

- **Single-based completion.** *For each compound*, add the minimal number of reactions in the network

ASP [Thiele'11]

- **Global-based completion.** Add the global minimum of reactions in the network required *for all compounds in the same time*

Application to an eukaryot example



Brown algae

- **Ectocarpus**. Model for brown macro-algae.
- **Specificities**. Very distant from well-studied green micro-algae.
- Capable of adaptation and acclimation.

Data [Station Biologique Roscoff]

- **Genome**. High-quality annotated genome.
- **Metabolism**. List of 56 characterized metabolic compounds.

Ectocarpus metabolism reconstruction

Reconstruction *[Prigent. Work in progress]*

- **Automatic tools.** Bad reconstruction.
- **Global cardinal completion.** **Adding 59 metabolic reactions allows producing 48 compounds over 56**
- **Single-based completion.** 38 reactions belong to all solutions.

Enumeration *[Prigent&Thiele. Work in progress]*

- **ASP.** Enumeration is possible.
- **Combinatorial explosion.** **The full set of possible completions contains 16 millions of solutions**
- **Reactions.** **About 100** reactions occur in at least one solution.
- **Performance.** High level of RAM. Extreme range of solvers.

Current issues

- **New biological metrics** to sort information !
- **Integration** Take advantage of the flexibility of the declarative language to insert new criteria of classification.
- Sampling the space of solution? *[Christian'11]*

Conclusion

Novelties brought declarative logic paradigms ??

High-level declarative language

→ Easy "step-by-step" encoding of data integration and constraints.

- Confrontation of a reconstructed network with additional data.
- Learn the logic quasi-steady state response of signaling networks.
- Completion of metabolic networks.

Enumeration of complete space of solutions

→ Explore the combinatorics responsible of the explosion of the size

- Global correction of transcriptional networks.
- Sub-optimal solutions to middle-case problems (learning the dynamics).
- Global set completion to metabolism reconstruction.

Work in Progress

- Biological criteria to elucidate the structure of the space of solutions.
- Sampling issues.
- ASP: backtrack traces of "proofs" to classify the importance of initial information.
- Software.

Acknowledgements

ASP Modelling

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